

Modeling and Analysis Principles for Chemical and Biological Engineers

Errata for First Printing

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December 7, 2025

- Page 5. Change y_n to y_m in second to last displayed equation. Thanks to Nishith Patel of UW for pointing out this erratum.
- Pages 7-8. In Example 1.4, matrix A is missing a minus sign. Replace A , AB and BA by the following:

$$A = \begin{bmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{bmatrix} \quad AB = \begin{bmatrix} \sqrt{2} & -\frac{1}{2\sqrt{2}} \\ \sqrt{2} & \frac{1}{2\sqrt{2}} \end{bmatrix} \quad BA = \begin{bmatrix} \sqrt{2} & -\sqrt{2} \\ \frac{1}{2\sqrt{2}} & \frac{1}{2\sqrt{2}} \end{bmatrix}$$

Thanks to Shu Pan of UW for pointing out this erratum.

- Page 12, line 13. Replace “outer project” with “outer product.” Thanks to Ted Walker of UW for pointing out this erratum.
- Page 15, first line change $b \in \mathbb{R}^n$ to $b \in \mathbb{R}^m$. Thanks to Apoorva Sampat of UW for pointing out this erratum.
- Page 37, 13 lines from bottom. Replace $Av_j = \lambda_j$ with $Av_j = \lambda_j v_j$. Thanks to Nishith Patel of UW for pointing out this erratum.
- Page 42. Item 5. Change $\Leftrightarrow B^T AB > 0$ to $\Rightarrow B^T AB > 0$. Thanks to Travis Arnold of UW for pointing out this erratum.
- Page 45. In second displayed equation, replace $e^{-\omega t}$ with $e^{-i\omega t}$. Thanks to Nishith Patel of UW for pointing out this erratum.
- Page 47, sixteen lines from the top. Replace the sentences:
“This fact can be established by noting that if complex-valued $q = a + bi$ is an eigenvector of A , then so are both real-valued vectors a and b . And if complex eigenvector q_j is orthogonal to q_k , then real eigenvectors a_j and b_j are orthogonal to real eigenvectors a_k and b_k , respectively.”
with the following:
“This fact can be established by specializing the results in Exercises 1.42 and 1.43 to real rather than complex matrices and noting that the eigenvalues are real.”
Thanks to Sally Jiao of UCSB for pointing out this erratum.
- Page 49. In fifth displayed equation, replace second S with S^* , and S^2 with SS^* . In sixth displayed equation, replace first S with S^* , and S^2 with S^*S .

- Page 49, six lines from bottom. Replace $m - n$ with $n - m$. Page 50, four lines from bottom. Replace $n - m$ with $m - n$. Thanks to Ralph White of Univ. of South Carolina for pointing out this erratum.
- Page 52, line after first displayed equation in Section 1.5.1. Change $i = 1, \dots, n$ to $i = 0, \dots, n$. Thanks to Sanjan Gupta of UW for pointing out this erratum.
- Page 55. Eighth line of the last full paragraph: replace “More generally, $\Lambda^{1/2}$ can be replaced by $Q^* \Lambda^{1/2} Q$ for any unitary matrix Q ” with “More generally, $\Lambda^{1/2}$ can be replaced by $\text{diag}(\pm \lambda_1^{1/2}, \pm \lambda_2^{1/2}, \dots)$.” Thanks to Coogan Thompson of UW for pointing out this issue.
- Page 60, second to last line of first paragraph. Change $A > 0$ to $A < 0$. Thanks to Sanjan Gupta of UW for pointing out this erratum.
- Page 68, first displayed equation. Change $\sigma(A \otimes B)$, $\sigma(A)$, and $\sigma(B)$, to $\sigma^2(A \otimes B)$, $\sigma^2(A)$, and $\sigma^2(B)$, respectively. Thanks to Sanjan Gupta of UW for pointing out this erratum.
- Page 72, Exercise 1.12. In part (a), change “ nn^T is the projection operator” to “ nn^T is a projection operator”.
- Page 78, Equation (1.31). Change the vector of input values to

$$\begin{bmatrix} u(n-1) \\ u(n-2) \\ \vdots \\ u(0) \end{bmatrix}$$

- Page 83. Exercise 1.45 (d). Change “largest eigenvalue” to “largest magnitude eigenvalue.” Thanks to Kimberlee Keithley of UCSB for pointing out this erratum.
- Page 95. For improved clarity, add the following to the end of Exercise 1.77 (d).

Note that for a matrix (like A) with linearly independent columns, the pseudoinverse is $A^\dagger = (A^T A)^{-1} A^T$, but for a matrix (like B) with linearly independent rows, the pseudoinverse is $B^\dagger = B^T (B B^T)^{-1}$. The matrices A^\dagger and B^\dagger are also known as left and right inverses, respectively.

Thanks to Megan Zagrobely of UW for pointing out this issue.

- Page 100. In the first equation, change $A^2 t$ to $A^2 t^2$, and change $A^3 t$ to $A^3 t^3$.
- Page 100. In the second equation change S to M . (Though in the case under consideration, where A is diagonalizable, M reduces to S as described in Chapter 1.)
- Page 100. In the last displayed equation, change $\text{Re}(c_1 e^{\sigma t} e^{i\omega t} v)$ to $2\text{Re}(c_1 e^{\sigma t} e^{i\omega t} v)$. Thanks to Sanjan Gupta of UW for pointing out this erratum.
- Page 101, first displayed equation. Change the sign on the 2nd and 4th terms of the sum on the right-hand side. Thanks to Sanjan Gupta of UW for pointing out this erratum.
- Page 107, Table 2.1. Change b to ω in last two entries. Thanks to Harmon Ray of UW for pointing out this erratum.

24. Page 109. Fourth line in the solution of Example 2.2. Replace $s + a$ with $s - a$ in the denominator of the first term on the right-hand side of the equation.
25. Page 114. In the first full paragraph, " $a_0 = 1, a_1 = -2, a_2 = 1$ " should read " $a_0 = 1, a_1 = -1, a_2 = 1$ ". Thanks to Ralph White of Univ. of South Carolina for pointing out this erratum.
26. Page 171. Fourth line in part (c). Change $t_f = t/k_{-1}$ to $t_f = k_{-1}t$. Thanks to Luo Ji of UW for pointing out this erratum.
27. Page 211. In the equation at the bottom of the page, change u_j to c_j . Thanks to Feifan Du of UW for pointing out this erratum.
28. Page 215. In the two equations at the bottom of the page, the sums should range from 0 to $n - 1$ and c_j should be replaced by c_{j+1} . Thanks to Maddie Pont of UW for pointing out this erratum.
29. Page 226, Exercise 2.20(b). The equation $\omega_1^2 + \omega_2^2 + \omega_3^2 = 1$ should be replaced by $I_1^2 \omega_1^2 + I_2^2 \omega_2^2 + I_3^2 \omega_3^2 = 1$.
30. Page 235, Exercise 2.44(b). Change $y(x)$ to $u(x)$.
31. Page 237, Exercise 2.49. For consistency with the text, vectors x_n, y_{n+M} etc. should be rewritten $x^{(n)}, y^{(n+M)}$ etc. Also, change A to G in part (b).
32. Page 237, Exercises 2.50 and 2.51. For consistency with the text, vectors x_n, u_n, v_n etc. should be rewritten $x^{(n)}, u^{(n)}, v^{(n)}$ etc.
33. Page 239, Exercise 2.54. This exercise has been updated. It should read

The eigenvalue problem

$$y'' + (x + \lambda)y = 0$$

arises in optics, quantum mechanics, and hydrodynamics, and is known as Airy's equation.

- (a) If only an estimate of the smallest (magnitude) eigenvalue λ is needed, a *one-term* Galerkin approximation can be useful. In quantum mechanics, where eigenvalues have the interpretation of energy levels, this approach is a version of the GROUND STATE APPROXIMATION. Use a one-term Galerkin approximation using a sine function basis, $\phi_j = \sin j\pi x$, to estimate the first eigenvalue of Airy's equation with boundary conditions $y(0) = y(1) = 0$. That is, let $y(x) \approx c_1 \sin \pi x$.
- (b) Repeat with a two-term Galerkin approximation, $y(x) \approx c_1 \sin \pi x + c_2 \sin 2\pi x$.
- (c) Use the finite element method with hat functions to construct an *algebraic* problem for the Airy equation: it will have the structure $Au + \lambda Bu = 0$. The matrix B will be invertible so this form can be converted to a standard algebraic eigenvalue problem. Find the approximate eigenvalues and eigenfunctions using six hat functions and again with 12.

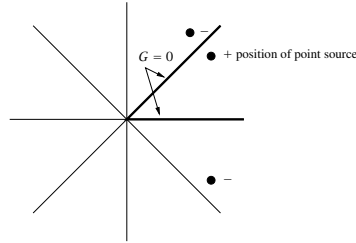
34. Page 260, Figure 3.2. Change δ_r, δ_θ to e_r, e_θ .

35. Page 261, displayed equation prior to (3.5). Change the final term in parentheses from

$$\frac{1}{r} \frac{\partial e_\theta}{\partial \theta} \frac{\partial}{\partial r} \quad \text{to} \quad \frac{1}{r} \frac{\partial e_\theta}{\partial \theta} \frac{\partial}{\partial \theta}$$

36. Page 263, Figure 3.3. Change $\delta_r, \delta_\theta, \delta_\phi$ to e_r, e_θ, e_ϕ .
37. Page 264, 8 lines from bottom. Replace $-e_y$ with $-e_x$ and $-e_x$ with $-e_y$. Thanks to Ralph White of Univ. of South Carolina for pointing out this erratum.
38. Page 268, 4th displayed equation. Remove the extraneous dV in the $\nabla \cdot F_A dV$ term in brackets. Thanks to Sanjan Gupta of UW for pointing out this erratum.
39. Page 279, Example 3.6. Three sign changes in last sentence: change $w_{xx} + w_{yy} = \lambda w$ to $w_{xx} + w_{yy} = -\lambda w$, and $\lambda_{mn} u_{mn} = f_{mn}$ to $-\lambda_{mn} u_{mn} = f_{mn}$, and $u_{mn} = f_{mn}/\lambda_{mn}$ to $u_{mn} = -f_{mn}/\lambda_{mn}$. Also, in the final equation of the example, change the index in the second summation from m to n .
40. Page 282, last three equations. In the arguments of the modified Bessel functions I_0 and K_0 , replace $n^2 \pi^2$ by $n\pi$.
41. Page 293, item 7. Replace $f(k)$ with $\hat{f}(k)$. Thanks to Chelsea Edwards of UCSB for pointing out this erratum.
42. Page 309, first displayed equation. In the denominator of a_{ni} , change $(r_n - 1)!$ to $(r_n - i)!$. The same erratum is on page 530 below.
43. Page 314, 3rd displayed line of solution. Change t to τ (two places). Thanks to David Podorefsky of UCSB for pointing out this erratum.
44. Page 314, last displayed equation. Remove both leading minus signs in the two cases of the $\bar{G}(x, \xi, s)$ expression. Thanks to Ahmed Elnabawy of UW for pointing out this and the next erratum.
45. Page 315, fourth displayed equation from the bottom. Replace $(-1)^n$ with $(-1)^{n+1}$ in the two cases of the $G(x, \xi, \tau)$ expression.
46. Page 317, second equation from the bottom. In the second term, the factor N should be removed and the summation should go from $j = 1$ to N . Thanks to Feifan Du of UW for pointing out this erratum.
47. Page 320, second equation from the bottom. Remove the factor Δt from the right-hand side. Thanks to Feifan Du of UW for pointing out this erratum.
48. Page 325, Exercise 3.1, line 10. Change $x_1 = 1$ to $x_1 = x$. Delete the extraneous sentence starting "The same arguments hold ..." to the end of the exercise.
49. Page 327, Exercise 3.13. Replace "These equations can be written in matrix-vector form as," with "These equations can be written in matrix-vector form as $AU = F$." Thanks to Chelsea Edwards of UCSB for pointing out this and the next erratum.
50. Page 327, Exercise 3.13. In the third displayed equation of the exercise, replace f with $-f$.

51. Page 339, Exercise 3.42. The images in the figure are not shown in a format consistent with the text. The correct figure appears as follows.



52. Page 341, Exercise 3.50, first sentence. Replace "...the plucked string initial condition, $u(x, 0) = u_0(x)$, $u_\tau(x, 0) = v(x)$," with "...the struck string initial condition, $u(x, 0) = 0$, $u_\tau(x, 0) = v(x)$." Thanks to Patrick Leggieri of UCSB for pointing out this erratum.
53. Page 343, Exercise 3.52. Replace "AM2" with "implicit Euler".
54. Page 343, Exercise 3.53. Replace "Adams-Moulton" with "implicit Euler", " $\alpha = 0.05$ " with " $\alpha = 0.1$ " and " $T(-1, 0) = 1$ " with " $T(-1, t) = 1$ ".
55. Pages 343 and 345. Replace "Levy" with "Lewy".
56. Pages 344, 348 and 568. Replace "Nicholson" with "Nicolson".
57. Page 355, Figure 4.1 should appear as shown here. Note the σ^2 labels are changed to σ in the figure (three places), and "variances" is changed to "standard deviations" in the caption.
58. Page 356, second displayed equation. Change e^{-itx} to e^{itx} . In the third displayed equation, change e^{-itz} to e^{itz} . Thanks to Ralph White of Univ. of South Carolina for pointing out this erratum.
59. Page 363, first displayed equation. Put absolute value around $\det Q$.
60. Page 377, Ninth line from top, "...and there is no random component ξ_2 ." Change to "...and there is no component ξ_1 ." Thanks to Travis Arnold of UW for pointing out this erratum.
61. Page 385, fourth displayed equation. Change $i\mathcal{E}(Y_i)$ term to $it\mathcal{E}(Y_i)$. Thanks to Travis Arnold of UW for pointing out this erratum.
62. Page 389, fifth displayed equation. Change $p_{\eta, \xi}$ on the left-hand side of the equality to $p_{\eta|\xi}$. Thanks to Travis Nelson of UW for pointing out this erratum.
63. Page 392, twelfth line from top. Change (4.20) to (4.40).
64. Page 393, sixth line from the bottom. Change maximize to maximizing.
65. Page 394, tenth line from top. Change $e_i = y_i - x_i^T \theta$ to $e_i = y_i - x_i^T \hat{\theta}$.

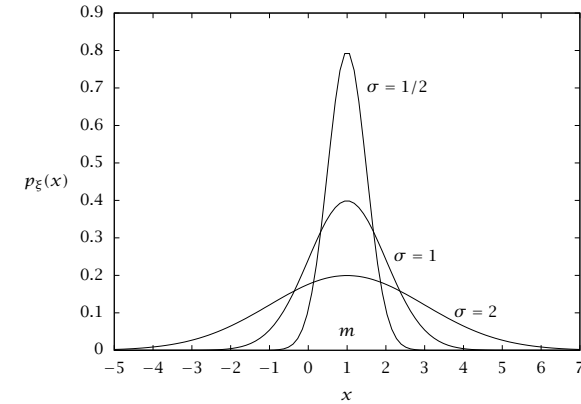


Figure 4.1: Normal distribution, with probability density $p_\xi(x) = (1/\sqrt{2\pi\sigma^2}) \exp(-(1/2)(x - m)^2/\sigma^2)$. Mean is one and standard deviations are 1/2, 1, and 2.

66. Page 398, Figure 4.10. The joint density in the top right plot is not correct. The corrected figure is shown here. Thanks to Ralph White of Univ. of South Carolina for pointing out this erratum.
67. Page 410, sixth line from top. Change $B^T B$ to BB^T .
68. Page 411, twelfth line from top. Change right-hand side from $R^{-2}C$ to $R^{-1}C^T R^{-1}$. Eighth line from bottom, change $\frac{1}{2}R^{-2} \sum_i (y_i - \Theta x_i)(y_i - \Theta x_i)^T$ to $\frac{1}{2}R^{-1} \left(\sum_i (y_i - \Theta x_i)(y_i - \Theta x_i)^T \right) R^{-1}$. Make this same change on page 414, third displayed equation from bottom.
69. Page 411, three lines from bottom. Change "The estimate \hat{R} is an unbiased estimate of the measurement variance R ." to "The estimate \hat{R} is a biased estimate of the measurement variance R with $\mathcal{E}(\hat{R}) = R(n - q)/n$."
70. Page 412, Equation 4.61. Change $p_W(W)$ to $p_W(W, n)$.
71. Page 414. Third displayed equation from bottom, change $\frac{1}{2}R^{-2} \sum_i (y_i - \Theta x_i)(y_i - \Theta x_i)^T$ to $\frac{1}{2}R^{-1} \left(\sum_i (y_i - \Theta x_i)(y_i - \Theta x_i)^T \right) R^{-1}$.
72. Page 419. In the displayed B_{PCR} equation, change the P_f^T to P_f .
73. Page 420. In the two lines preceding the B_{PLS} displayed equation, change R to P (two places).
74. Page 447, Exercise 4.45. Change $F(n, p, \alpha)$ to $F(p, n, \alpha)$ in second displayed equation.

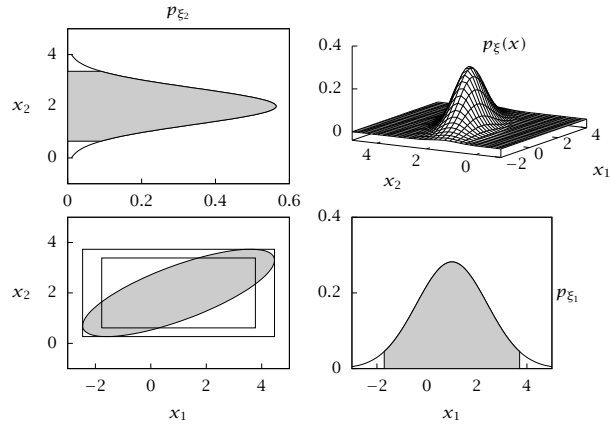


Figure 4.10: The multivariate normal density (top right). The two marginal densities and marginal 95% confidence regions (shaded) (top left and bottom right). The joint elliptical 95% confidence region (shaded), bounding box (outer), and the marginal box (inner) (bottom left).

75. Page 447, third line from bottom. Change Exercise 4.34 to Exercise 4.44.
76. Page 458, line before 4th displayed equation. Change $G = \sqrt{2D}$ to $G = \sqrt{2D\Delta t}$. Thanks to Sanjan Gupta of UW for pointing out this erratum.
77. Page 465. In Equation 5.18 and on the line following it, change $\Delta W(t + \Delta t)$ to $\Delta W(\Delta t)$.
78. Page 466, $df(x(t)) = f(x(t+dt)) - f(x(t))$ should be $df(x(t)) = f(x(t+dt)) - f(x(t))$, i.e., move the closing parenthesis.
79. Page 472, Equation 5.40. Change $\mathcal{A} \cdot \mathbf{x}(t)dt$ to $\mathcal{A}(\mathbf{x}, t)dt$.
80. Page 467, ten lines from bottom. Change $\sin \theta B dW_y$ to $\sin \theta dW_y$. Thanks to Titus Quah of UCSB for pointing out this erratum.
81. Page 478, end of sentence before final paragraph. Change $\lambda = V/Q$ to $\lambda = Q/V$. Thanks to Mike Doherty of UCSB for pointing out this erratum.
82. Pages 484 and 485, step 3 on both pages. Add minus signs in front of the corresponding $(1/r) \ln u$ terms. Thanks to Yuliya Preger of UW for pointing out these errata.
83. Page 487, Equation 5.54. Change the minus sign in front of the $k_{-1}(c_0 + \varepsilon)$ term to a plus sign. Thanks to Apoorva Sampat of UW for pointing out this erratum.
84. Page 492, change $r_1(x) = k_1 n_A$ to $r_1(x) = k_1 n_A n_B$ in first displayed equation. Change $k_1(n_A + 1)$ to $k_1(n_A + 1)(n_B + 1)$ and change $k_1 n_A$ to $k_1 n_A n_B$ in second displayed equation.

85. Page 493, 7th line. Change ξ to ε .
86. Page 506, first line of second boxed equation. Change $p_{x(k)|y(k-1)}(x(k+1)|y(k))$ to $p_{x(k)|y(k-1)}(x(k)|y(k-1))$.
87. Page 530, Table A.1. Last line on page 530. In the denominator of a_{ni} , change $(r_n - 1)!$ to $(r_n - i)!$.